

# Online Algebra, Logic, and Topology Seminar

Category Theory Seminar — Abstract

October 07, 2025

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## When are exact categories co-exact?

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**Speaker:** James Gray

*Stellenbosch University, South Africa*

**Date & Time:** October 07, 2025 (Tuesday) — 3:00 PM (Coimbra time)

**Place:** Google Meet

**Abstract.** The aim of the talk is two-fold: (i) to explain that finitely co-complete pretoposes are co-ideally-exact [J] and co-arithmetical [P], and (ii) to explain that there are conditions in common between additive and lexensive categories, which together with exactness (and finite cocompleteness) imply co-exactness and co-protomodularity. As a consequence of (i) we recover Theorem 1.3 of [BC] which states that the dual of the category of pointed compact Hausdorff spaces is semi-abelian, which in fact was the motivation to begin this work.

## References

- [BC] F. Borceux, M.M. Clementino, *On toposes, algebraic theories, semi-abelian categories and compact Hausdorff spaces*, Theory and Applications of Categories 43(11), 363–381, 2025.
- [J] G. Janelidze, *Ideally exact categories*, Theory and Applications of Categories 41(11), 414–425, 2024.
- [P] M.C. Pedicchio, *A categorical approach to commutator theory*, Journal of Algebra 177, 647–657, 1995.